

# Package ‘ProjectionBasedClustering’

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**Type** Package

**Title** Projection Based Clustering

**Version** 1.2.1

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**Description** A clustering approach applicable to every projection method is proposed here. The two-dimensional scatter plot of any projection method can construct a topographic map which displays unapparent data structures by using distance and density information of the data. The generalized U\*-matrix renders this visualization in the form of a topographic map, which can be used to automatically define the clusters of high-dimensional data. The whole system is based on Thrun and Ultsch, “Using Projection based Clustering to Find Distance and Density based Clusters in High-Dimensional Data” <[DOI:10.1007/s00357-020-09373-2](https://doi.org/10.1007/s00357-020-09373-2)>. Selecting the correct projection method will result in a visualization in which mountains surround each cluster. The number of clusters can be determined by counting valleys on the topographic map. Most projection methods are wrappers for already available methods in R. By contrast, the neighbor retrieval visualizer (NeRV) is based on C++ source code of the 'dredviz' software package, the t-SNE multicore version is based on C++ source code of Dmitry Ulyanov, and the Curvilinear Component Analysis (CCA) is translated from 'MATLAB' ('SOM Toolbox' 2.0) to R.

**License** GPL-3

**Imports** Rcpp, ggplot2, stats, graphics, vegan, deldir, geometry, GeneralizedUmatrix, shiny, shinyjs, shinythemes, plotly, grDevices

**Suggests** DataVisualizations, fastICA, tsne, FastKNN, MASS, pcaPP, spdep, pracma, grid, mgcv, fields, png, reshape2, Rtsne, methods, dendextend, umap, uwot, DatabionicSwarm, parallelDist, parallel

**LinkingTo** Rcpp

**LazyData** TRUE

**Encoding** UTF-8

**SystemRequirements** C++17

**Depends** R (>= 3.0)

**NeedsCompilation** yes

**URL** <https://www.deepbionics.org>

**LazyLoad** yes

**BugReports** <https://github.com/Mthrun/ProjectionBasedClustering/issues>

**Author** Michael Thrun [aut, cre, cph],  
 Quirin Stier [ctb, rev] (<<https://orcid.org/0000-0002-7896-4737>>),  
 Brinkmann Luca [ctb],  
 Florian Lerch [aut],  
 Felix Pape [aut],  
 Tim Schreier [aut],  
 Luis Winckelmann [aut],  
 Kristian Nybo [cph],  
 Jarkko Venna [cph],  
 Ulyanov Dimitry [cph],  
 van der Maaten Laurens [cph]

**Maintainer** Michael Thrun <m.thrun@gmx.net>

**Repository** CRAN

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ProjectionBasedClustering-package

*Projection Based Clustering*

---

## Description

The package is based on a conference talk [Thrun/Ultsch, 2017], see <DOI:10.13140/RG.2.2.13124.53124>. and [Thrun/Ultsch, 2020]. The abstract of the conference talk is as follows:

Many data mining methods rely on some concept of the dissimilarity between pieces of information encoded in the data of interest. These methods can be used for cluster analysis. However, no generally accepted definition of clusters exists in the literature [Hennig et al., 2015]. Here, consistent with Bouveyron et al., it is assumed that a cluster is a group of similar objects [Bouveyron et al., 2012]. The clusters are called natural because they do not require a dissection; instead, they are clearly separated in the data [Duda et al., 2001, Theodoridis/Koutroumbas, 2009, pp. 579, 600]. These clusters can be identified by distance or density based high-dimensional structures. Dimensionality reduction techniques are able to reduce the dimensions of the input space to facilitate the exploration of structures in high-dimensional data. If they are used for visualization, they are called projection methods. The generalized U\*-matrix technique is applicable for these and can be used to visualize both distance- and density-based structures [Thrun 2018; Ultsch/Thrun, 2017]. The idea that the abstract U\*-matrix (AU-matrix) can be used for clustering [Ultsch et al., 2016]. The distances required for hierarchical clustering are defined by the AU-matrix [Lötsch/Ultsch, 2014]. Using this distance we propose a clustering approach for every projection method based on the U\*-matrix visualization of a topographic map [Thrun 2018; Thrun/Ultsch, 2017]. The number of clusters and the cluster structure can be estimated by counting the valleys in a topographic map [Thrun et al., 2016]. If the number of clusters and the clustering method are chosen correctly, then the clusters will be well separated by mountains in the visualization. Outliers are represented as volcanoes and can be interactively marked in the visualization after the automated clustering process.

Furthermore, [Thrun et al., 2021] presents an interactive parameter-free approach, that incorporates a human-in-the-loop, for projection-based clustering.

## Details

A comparison to 32 common clustering algorithms is provided in [Thrun/Ultsch, 2020].

## Note

If you want to verify your clustering result externally, you can use Heatmap or SilhouettePlot of the CRAN package DataVisualizations.

Additionally you can use the standard ShepardScatterPlot or the better approach through the ShepardDensityPlot of the CRAN package DataVisualizations.

## Author(s)

Michael Thrun, Felix Pape, Florian Lerch, Tim Schreier, Luis Winckelmann

## References

- [Thrun/Ultsch, 2017] Thrun, M.C., Ultsch, A.: Projection based Clustering, Conf. Int. Federation of Classification Societies (IFCS),DOI:10.13140/RG.2.2.13124.53124, Tokyo, 2017.
- [Bouveyron et al., 2012] Bouveyron, C., Hammer, B., & Villmann, T.: Recent developments in clustering algorithms, Proc. ESANN, Citeseer, 2012.
- [Duda et al., 2001] Duda, R. O., Hart, P. E., & Stork, D. G.: Pattern classification, (Second Edition ed.), Ney York, USA, John Wiley & Sons, ISBN: 0-471-05669-3, 2001.
- [Hennig et al., 2015] Hennig, C., Meila, M., Murtagh, F., & Rocci, R.: Handbook of cluster analysis, New York, USA, CRC Press, ISBN: 9781466551893, 2015.
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- [Theodoridis/Koutroumbas, 2009] Theodoridis, S., & Koutroumbas, K.: Pattern Recognition, (Fourth Edition ed.), Canada, Elsevier, ISBN: 978-1-59749-272-0, 2009.
- [Thrun et al., 2016] Thrun, M. C., Lerch, F., Lötsch, J., & Ultsch, A.: Visualization and 3D Printing of Multivariate Data of Biomarkers, in Skala, V. (Ed.), International Conference in Central Europe on Computer Graphics, Visualization and Computer Vision (WSCG), Vol. 24, Plzen, <http://wscg.zcu.cz/wscg2016/short/A43-full.pdf>, 2016.
- [Ultsch et al., 2016] Ultsch, A., Behnisch, M., & Lötsch, J.: ESOM Visualizations for Quality Assessment in Clustering, In Merényi, E., Mendenhall, J. M. & O’Driscoll, P. (Eds.), Advances in Self-Organizing Maps and Learning Vector Quantization: Proceedings of the 11th International Workshop WSOM 2016, Houston, Texas, USA, January 6-8, 2016, (10.1007/978-3-319-28518-4\_3pp. 39-48), Cham, Springer International Publishing, 2016.
- [Ultsch/Thrun, 2017] Ultsch, A., & Thrun, M. C.: Credible Visualizations for Planar Projections, in Cottrell, M. (Ed.), 12th International Workshop on Self-Organizing Maps and Learning Vector Quantization, Clustering and Data Visualization (WSOM), IEEE Xplore, France, 2017.
- [Thrun/Ultsch, 2020] Thrun, M. C., & Ultsch, A.: Using Projection based Clustering to Find Distance and Density based Clusters in High-Dimensional Data, Journal of Classification, Vol. 38(2), pp. 280-312, Springer, DOI: 10.1007/s00357-020-09373-2, 2020.
- [Thrun et al., 2021] Thrun, M. C., Pape, F. & Ultsch, A.: Conventional displays of structures in data compared with interactive projection-based clustering (IPBC), International Journal of Data Science and Analytics, Vol. 12(3), pp. 249-271, Springer, DOI: 10.1007/s41060-021-00264-2, 2021

## Examples

```
data('Hepta')
#2d projection
# Visualizuation of GeneralizedUmatrix

projectionpoints=NeRV(Hepta$Data)
#Computation of Generalized Umatrix
library(GeneralizedUmatrix)
visualization=GeneralizedUmatrix(Data = Hepta$Data,projectionpoints)
TopviewTopographicMap(visualization$Umatrix,visualization$Bestmatches)
```

```

#or in 3D if rgl package exists
#plotTopographicMap(visualization$Umatrix,visualization$Bestmatches)

##Interactive Island Generation
## from a tiled Umatrix (toroidal assumption)
## Not run:
Imx = ProjectionBasedClustering::interactiveGeneralizedUmatrixIsland(visualization$Umatrix,
visualization$Bestmatches)
#plotTopographicMap(visualization$Umatrix,visualization$Bestmatches, Imx = Imx)

## End(Not run)

# Automatic Clustering
LC=c(visualization$Lines,visualization$Columns)
# number of Cluster from dendrogram or visualization (PlotIt=TRUE)
Cls=ProjectionBasedClustering(k=7, Hepta$Data,

visualization$Bestmatches, LC,PlotIt=TRUE)
# Verification
library(GeneralizedUmatrix)
TopviewTopographicMap(visualization$Umatrix,visualization$Bestmatches,Cls)
#or in 3D if rgl package exists
#plotTopographicMap(visualization$Umatrix,visualization$Bestmatches,Cls)

## Sometimes you can improve a Clustering interactively or mark additional Outliers manually
## Not run:
Cls2 = interactiveClustering(visualization$Umatrix, visualization$Bestmatches, Cls)

## End(Not run)

```

---

CCA

---

*Curvilinear Component Analysis (CCA)*


---

## Description

CCA Projects data vectors using Curvilinear Component Analysis [Demartines/Herault, 1995],[Demartines/Herault, 1997].

Unknown values (NaN's) in the data: projections of vectors with unknown components tend to drift towards the center of the projection distribution. Projections of totally unknown vectors are set to unknown (NaN).

## Usage

```

CCA(DataOrDistances,Epochs,OutputDimension=2,method='euclidean',

alpha0 = 0.5, lambda0,PlotIt=FALSE,Cls)

```

**Arguments**

DataOrDistances	Numerical matrix defined as either Data, i.e., [1:n,1:d], nonsymmetric, and consists of n cases of d-dimensional data points with every case having d attributes, variables or features, or Distances, i.e.,[1:n,1:n], symmetric and consists of n cases, e.g., as <code>matrix(dist(Data,method))</code>
Epochs	Number of eppochs (scalar), i.e, training length
OutputDimension	Number of dimensions in the Outputspace, default=2
method	method specified by distance string. One of: 'euclidean', 'cityblock=manhattan', 'cosine', 'chebychev', 'jaco
alpha0	(scalar) initial step size, 0.5 by default
lambda0	(scalar) initial radius of influence, $3 \cdot \max(\text{std}(D))$ by default
PlotIt	Default: FALSE, If TRUE: Plots the projection as a 2d visualization. OutputDimension>2: only the first two dimensions will be shown
Cls	[1:n,1] Optional,; only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.

**Details**

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

A n by OutputDimension matrix containing coordinates of the projected points.

**Note**

Only Transferred from matlab to R. Matlabversion: Contributed to SOM Toolbox 2.0, February 2nd, 2000 by Juha Vesanto.

You can use the standard Sheparddiagram or the better approach through the ShepardDensityScatter of the CRAN package DataVisualizations.

**Author(s)**

Florian Lerch

**References**

[Demartines/Herault, 1997] Demartines, P., & Herault, J.: Curvilinear component analysis: A self-organizing neural network for nonlinear mapping of data sets, IEEE Transactions on Neural Networks, Vol. 8(1), pp. 148-154. 1997.

[Demartines/Herault, 1995] Demartines, P., & Herault, J.: CCA:" Curvilinear component analysis", Proc. 15 Colloque sur le traitement du signal et des images, Vol. 199, GRETSI, Groupe d'Etudes du Traitement du Signal et des Images, France 18-21 September, 1995.

**Examples**

```
data('Hepta')
Data=Hepta$Data

Proj=CCA(Data,Epochs=20)

## Not run:
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)
```

---

ContTrustMeasure	<i>Measure of trustworthiness and continuity for projection</i>
------------------	---

---

**Description**

Computes trustworthiness and continuity for projected data (see [Kaski2003]).

**Usage**

```
ContTrustMeasure(datamat, projmat, lastNeighbor)
```

**Arguments**

datamat	numerical matrix of data: n cases in rows, d variables in columns
projmat	numerical matrix of projected data: n cases in rows, k variables in columns, where k is the projection output dimension
lastNeighbor	scalar, maximal size of neighborhood to be considered

**Details**

C++ source code comes from <https://research.cs.aalto.fi/pml/software/dredviz/>

**Value**

numerical [k,7] matrix, where k is the lastNeighbor value. The matrix contains the columns:  
Neighborhood size; worst-case trustworthiness; average trustworthiness; best-case trustworthiness;  
worst-case continuity; average continuity; best-case continuity

where neighborhood size is the size of the neighborhood considered, which ranges from 1:lastNeighbor

**Author(s)**

Michael Thrun

## References

[Kaski2003]: Samuel Kaski, Janne Nikkilä, Merja Oja, Jarkko Venna, Petri Törönen, and Eero Castren. Trustworthiness and metrics in visualizing similarity of gene expression. *BMC Bioinformatics*, 4:48, 2003.

## See Also

An alternative measure is the [KLMeasure](#)

## Examples

```
data('Hepta')
Data=Hepta$Data
res=MDS(Data)
Proj = res$ProjectedPoints
PlotProjectedPoints(res$ProjectedPoints,Hepta$Cls)

ContTrustMeasure(Hepta$Data, Proj, 10)
```

---

DefaultColorSequence    *Default color sequence for plots*

---

## Description

Defines the default color sequence for plots made within the Projections package.

## Usage

```
data("DefaultColorSequence")
```

## Format

A vector with 562 different strings describing colors for plots.

---

Delaunay4Points    *Adjacency matrix of the delaunay graph for BestMatches of Points*

---

## Description

Calculates the adjacency matrix of the delaunay graph for BestMatches (BMs) in tiled form if BestMatches are located on a toroid grid

## Usage

```
Delaunay4Points(Points, IsToroid = TRUE, Grid=NULL, PlotIt=FALSE)
```



**Arguments**

Points	[1:n,1:3] matrix containing the BMKey, X and Y coordinates of the n, Best-Matches NEED NOT BE UNIQUE, however, there is an edge in the Deaunay between duplicate points!
IsToroid	OPTIONAL, logical, indicating if BM's are on a toroid grid. Default is True
Grid	OPTIONAL, A vector of length 2, containing the number of lines and columns of the Grid
PlotIt	OPTIONAL, bool, Plots the graph

**Details**

as

**Value**

Delaunay[1:n,1:n] adjacency matrix of the Delaunay-Graph

**Author(s)**

Michael Thrun

**References**

[Thrun, 2018] Thrun, M. C.: Projection Based Clustering through Self-Organization and Swarm Intelligence, doctoral dissertation 2017, Springer, ISBN: 978-3-658-20539-3, Heidelberg, 2018.

---

DijkstraSSSP

*Dijkstra SSSP*

---

**Description**

Dijkstra's SSSP (Single source shortest path) algorithm:

gets the shortest path (geodesic distance) from source vertice(point) to all other vertices(points) defined by the edges of the adjasency matrix

**Usage**

DijkstraSSSP(Adj, Costs, source)

**Arguments**

Adj	[1:n,1:n] 0/1 adjascency matrix, e.g. from delaunay graph or gabriel graph
Costs	[1:n,1:n] matrix, distances between n points (normally euclidean)
source	int, vertice(point) from which to calculate the geodesic distance to all other points

**Details**

Preallocating space for DataStructures accordingly to the maximum possible number of vertices which is fixed set at the number 10001.

**Value**

ShortestPaths[1:n] vector, shortest paths (geodesic) to all other vertices including the source vertice itself

**Note**

runs in  $O(E \cdot \log(V))$

**Author(s)**

Michael Thrun

**References**

uses a changed code which is inspired by Shreyans Sheth 28.05.2015, see <https://ideone.com/qkmt31>

---

Hepta

*Hepta is part of the Fundamental Clustering Problem Suit (FCPS)*  
*[Thrun/Ultsch, 2020].*

---

**Description**

clearly defined clusters, different variances

**Usage**

```
data("Hepta")
```

**Details**

Size 212, Dimensions 3, stored in Hepta\$Data

Classes 7, stored in Hepta\$Cls

**References**

[Thrun/Ultsch, 2020] Thrun, M. C., & Ultsch, A.: Clustering Benchmark Datasets Exploiting the Fundamental Clustering Problems, Data in Brief, Vol. 30(C), pp. 105501, DOI 10.1016/j.dib.2020.105501, 2020.

**Examples**

```
data(Hepta)  
str(Hepta)
```

---

ICA *Independent Component Analysis (ICA)*

---

**Description**

Independent Component Analysis:

Negentropie: difference of entropy to a corresponding normally-distributed random variable  $J(y) = E(G(y) - E(G(v)))^2$

**Usage**

```
ICA(Data, OutputDimension=2, Contrastfunction="logcosh",
     Alpha=1, Iterations=200, PlotIt=FALSE, Cls)
```

**Arguments**

Data	numerical matrix of n cases in rows, d variables in columns, matrix is not symmetric.
OutputDimension	Number of dimensions in the Outputspace, default=2
Contrastfunction	Maximierung der Negentropie ueber geeignete Kontrastfunktion Default: 'logcosh' $G(u) = 1/a * \log \cosh(a*u)$ 'exp': $G(u) = -\exp(u^2/2)$
Alpha	constant with $1 \leq \alpha \leq 2$ used in approximation to neg-entropy when fun == "logcosh"
Iterations	maximum number of iterations to perform.
PlotIt	Default: FALSE, If TRUE: Plots the projection as a 2d visualization. OutputDimension>2: only the first two dimensions will be shown
Cls	[1:n,1] Optional,; only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.

**Details**

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

ProjectedPoints	[1:n,OutputDimension], n by OutputDimension matrix containing coordinates of the Projectio
Mixing	[1:OutputDimension,1:d] Mischungsmatrix s.d gilt $Data = MixingMatrix * ProjectedPoints$
Unmixing	Entmischungsmatrix with $Data * Unmixing = ProjectedPoints$
PCMatrix	pre-whitening matrix that projects data onto the first n.comp principal components.

**Note**

A wrapper for [fastICA](#)

You can use the standard ShepardScatterPlot or the better approach through the ShepardDensityPlot of the CRAN package DataVisualizations.

**Author(s)**

Michael Thrun

**Examples**

```
data('Hepta')
Data=Hepta$Data

Proj=ICA(Data)

## Not run:
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)
```

---

interactiveClustering *GUI for interactive cluster analysis*

---

**Description**

This tool is an interactive shiny tool that visualizes a given generalized Umatrix and allows the user to select areas and mark them as clusters to improve a projection based clustering.

**Arguments**

Umatrix	[1:Lines,1:Columns] Matrix of Umatrix Heights
Bestmaches	[1:n,1:2] Array with positions of Bestmatches
Cls	[1:n] Classification of the Bestmatches

**Details**

Clicking on "Quit" returns the Cls vector to the workspace.

**Value**

List of

- EnlargedUmatrix  
[1:Lines,1:Columns] Matrix of Umatrix Heights taken four times and arranged in a square 2x2.
- EnlargedBestmaches  
[1:n,1:2] Array with positions of Bestmatches according to the enlarged umatrix.

EnlargedCls	[1:n] Classification of the Bestmatches according to the enlarged umatrix.
Umatrix	[1:Lines,1:Columns] Matrix of Umatrix Heights
Bestmaches	[1:n,1:2] Array with positions of Bestmatches
Cls	[1:n] Classification of the Bestmatches
TopView_TopographicMap	Plot of a topographic map.

### Note

If you want to verify your clustering result externally, you can use Heatmap or SilhouettePlot of the CRAN package DataVisualizations.

### Author(s)

Florian Lerch, Michael Thrun

### References

[Thrun/Ultsch, 2017] Thrun, M.C., Ultsch, A.: Projection based Clustering, Conf. Int. Federation of Classification Societies (IFCS),DOI:10.13140/RG.2.2.13124.53124, Tokyo, 2017.

[Thrun, 2018] Thrun, M. C.: Projection Based Clustering through Self-Organization and Swarm Intelligence, doctoral dissertation 2017, Springer, Heidelberg, ISBN: 978-3-658-20539-3, doi:10.1007/9783658205409, 2018.

### Examples

```
data('Hepta')
#2d projection
# Visualizuation of GeneralizedUmatrix

projectionpoints=NeRV(Hepta$Data)
#Computation of Generalized Umatrix
library(GeneralizedUmatrix)
visualization=GeneralizedUmatrix(Data = Hepta$Data,projectionpoints)

## Semi-Automatic Clustering done interactively in a shiny gui
## Not run:
Cls = interactiveClustering(visualization$Umatrix, visualization$Bestmatches)
##Plotting
plotTopographicMap(visualization$Umatrix,visualization$Bestmatches,Cls)

## End(Not run)
```

---

interactiveGeneralizedUmatrixIsland  
*GUI for cutting out an Island.*

---

### Description

The toroid Umatrix is usually drawn 4 times, so that connected areas on borders can be seen as a whole. An island is a manual cutout of such a tiled visualization, that is selected such that all connected areas stay intact. This shiny tool allows the user to do this manually.

### Usage

```
interactiveGeneralizedUmatrixIsland(Umatrix, Bestmatches=NULL, CIs=NULL, Plotter="plotly")
```

### Arguments

Umatrix	[1:Lines,1:Columns] Matrix of Umatrix Heights
Bestmatches	[1:n, 1:2] Matrix with positions of Bestmatches for n datapoints, first columns is the position in Lines and second column in Columns
CIs	Classification of the Bestmatches
Plotter	Choose between plotting frameworks: "plotly" and "ggplot2"

### Details

Clicking on "Quit" returns the Imx matrix to the workspace. Details can be read in [Thrun et al, 2016, Thrun/Ultsch, 2017].

### Value

Boolean Matrix that represents the island within the tiled Umatrix.

### Note

This function is a deprecated version of a function from the Umatrix packages created by Florian Lerch and Michael Thrun

### Author(s)

Michael Thrun

### References

[Thrun, et al.,2016] Thrun, M. C., Lerch, F., Loetsch, J., Ultsch, A.: Visualization and 3D Printing of Multivariate Data of Biomarkers, in Skala, V. (Ed.), International Conference in Central Europe on Computer Graphics, Visualization and Computer Vision,Plzen, 2016.

[Thrun/Ultsch, 2017] Thrun, M.C., Ultsch, A.: Projection based Clustering, Conf. Int. Federation of Classification Societies (IFCS),<DOI:10.13140/RG.2.2.13124.53124>, Tokyo, 2017.

**Examples**

```

data("Hepta")
Data=Hepta$Data
Cls=Hepta$Cls
InputDistances=as.matrix(dist(Data))
res=cmdscale(d=InputDistances, k = 2, eig = TRUE, add = FALSE, x.ret = FALSE)
ProjectedPoints=as.matrix(res$points)
#see also ProjectionBasedClustering package for other common projection methods

library(GeneralizedUmatrix)
resUmatrix=GeneralizedUmatrix(Data,ProjectedPoints)
TopviewTopographicMap(resUmatrix$Umatrix,resUmatrix$Bestmatches,Cls)
#or in 3D if rgl package exists
#plotTopographicMap(resUmatrix$Umatrix,resUmatrix$Bestmatches,Cls)

##Interactive Island Generation
## from a tiled Umatrix (toroidal assumption)

## Not run:
Imx = interactiveGeneralizedUmatrixIsland(resUmatrix$Umatrix,
resUmatrix$Bestmatches)
plotTopographicMap(resUmatrix$Umatrix,
resUmatrix$Bestmatches, Imx = Imx)

## End(Not run)

```

---

interactiveProjectionBasedClustering

*Interactive Projection-Based Clustering (IPBC)*

---

**Description**

An interactive clustering tool published in [Thrun et al., 2020] that uses the topographic map visualizations of the generalized U-matrix and a variety of different projection methods. This function receives a dataset and starts a shiny interface where one is able to choose a projection method and generate a plot.ly visualization of the topographic map [Thrun et al., 2016] of the generalized U-matrix [Ultsch/Thrun, 2017] combined with projected points. It includes capabilities for interactive clustering within the interface as well as automatic projection-based clustering based on [Thrun/Ultsch, 2020].

**Usage**

```
interactiveProjectionBasedClustering(Data, Cls=NULL)
```

```
IPBC(Data, Cls=NULL)
```

**Arguments**

Data	The dataset [1:n,1:d] of n cases and d variables with which the U-matrix and the projection will be calculated. Please see also the note below.
Cls	Optional: Prior Classification of the data for the [1:n] cases of k classes.

**Details**

To cluster data interactively, i.e., select specific data points and create a cluster), first generate the visualization. Thereafter, switch in the menu to clustering, hold the left mouse button and then frame a valley. Simple mouse clicks will not start the lasso functionality of plotly.

The resulting clustering is stored in Cls which is a numerical vector of the length n (number of cases) with the integer elements of numbers from 1 to k if k is the number of groups in the data. Each element of Cls as an unambiguous mapping to a case of Data indicating by the rownames of Data. If Data has no rownames a vector from 1:n is generated and then Cls is named by it.

**Value**

Returns a List of:

Cls	[1:n] numerical vector of the clustering of the dataset for then cases of k clusters
Umatrix	[1:Lines,1:Columns] generalized Umatrix to be plotted, numerical matrix storing the U-heights, see [Thrun, 2018] for definition.
Bestmatches	[1:n,2] Matrix of GridConverted Projected Points [1:n, 1:2] called Bestmatches that defines positions for n datapoints, first columns is the position in Lines and second column in Columns
LastProjectionMethodUsed	name of last projection method that was used as a string
TopView_TopographicMap	The final plot generated by plot.ly when closing the tool

**Note**

Some dimensionality reduction methods will assume data without missing values, some other DR methods assume unique data points, i.e., no distance=0 for any two cases(rows) of data. In these cases the IPBC method will crash.

**Author(s)**

Tim Schreier, Felix Pape, Luis Winckelmann, Michael Thrun

**References**

[Ultsch/Thrun, 2017] Ultsch, A., & Thrun, M. C.: Credible Visualizations for Planar Projections, in Cottrell, M. (Ed.), 12th International Workshop on Self-Organizing Maps and Learning Vector Quantization, Clustering and Data Visualization (WSOM), IEEE Xplore, France, 2017.

[Thrun/Ultsch, 2017] Thrun, M. C., & Ultsch, A. : Projection based Clustering, Proc. International Federation of Classification Societies (IFCS), pp. 250-251, Japanese Classification Society (JCS), Tokyo, Japan, 2017.



[Thrun/Ultsch, 2020] Thrun, M. C., & Ultsch, A.: Using Projection based Clustering to Find Distance and Density based Clusters in High-Dimensional Data, *Journal of Classification*, Springer, DOI: 10.1007/s00357-020-09373-2, 2020.

[Thrun et al., 2020] Thrun, M. C., Pape, F., & Ultsch, A.: Interactive Machine Learning Tool for Clustering in Visual Analytics, 7th IEEE International Conference on Data Science and Advanced Analytics (DSAA 2020), pp. 672-680, DOI 10.1109/DSAA49011.2020.00062, IEEE, Sydney, Australia, 2020.

## Examples

```
if(interactive()){
  data('Hepta')
  Data=Hepta$Data

  V=interactiveProjectionBasedClustering(Data)

  # with prior classification
  Cls=Hepta$Cls
  V=IPBC(Data,Cls)
}
```

---

Isomap

*Isomap*

---

## Description

Isomap projection as introduced in 2000 by Tenenbaum, de Silva and Langford

Even with a manifold structure, the sampling must be even and dense so that dissimilarities along a manifold are shorter than across the folds. If data do not have such a manifold structure, the results are very sensitive to parameter values.

## Usage

```
Isomap(Distances,k,OutputDimension=2,PlotIt=FALSE,Cls)
```

## Arguments

Distances	Symmetric [1:n,1:n] distance matrix, e.g. as <code>matrix(dist(Data,method))</code>
k	number of k nearest neighbors, if the data is fragmented choose an higher k
OutputDimension	Number of dimensions in the output space, default = 2
PlotIt	Default: FALSE, If TRUE: Plots the projection as a 2d visualization. If OutputDimension > 2 only the first two dimensions will be shown.
Cls	Optional and only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.

**Details**

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

ProjectedPoints[1:n,OutputDimension] n by OutputDimension matrix containing coordinates of the Projection: A matrix of the fitted configuration..

**Note**

A wrapper enabling a planar projection of the manifold learning method based on the isomap of the package vegan

if Data fragmented choose an higher k

You can use the standard ShepardScatterPlot or the better approach through the ShepardDensityPlot of the CRAN package DataVisualizations.

**Author(s)**

Michael Thrun

**Examples**

```
data('Hepta')
Data=Hepta$Data

Proj=Isomap(as.matrix(dist(Data)),k=7)

## Not run:
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)
```

---

KLMeasure

*Rank-based smoothed precision/recall measure for projection.*

---

**Description**

Computes rank-based smoothed precision/recall, with cost function based on Kullback-Leibler-divergence (see [Venna2010]).

**Usage**

```
KLMeasure(Data, pData, NeighborhoodSize = 20L)
```

**Arguments**

Data numerical matrix of data: n cases in rows, d variables in columns  
pData numerical matrix of projected data: n cases in rows, k variables in columns,  
where k is the projection output dimension  
NeighborhoodSize Number of points in neighborhood to be considered. Default is 20

**Value**

SmoothedPrecision Scalar, smoothed precision value  
SmoothedRecall Scalar, smoothed recall value

**Note**

C++ source code comes from <https://research.cs.aalto.fi/pml/software/dredviz/>

**Author(s)**

Michael Thrun

**References**

[Venna2010]: Jarkko Venna, Jaakko Peltonen, Kristian Nybo, Helena Aidos, and Samuel Kaski. Information Retrieval Perspective to Nonlinear Dimensionality Reduction for Data Visualization. Journal of Machine Learning Research, 11:451-490, 2010.

**See Also**

An alternative measure is the [ContTrustMeasure](#)

**Examples**

```
data('Hepta')
Data=Hepta$Data
res=MDS(Data)
Proj = res$ProjectedPoints

kl_m = KLMeasure(Hepta$Data, Proj)
# Smoothed precision
print(kl_m[[1]])
# Smoothed recall
print(kl_m[[2]])
```

KruskalStress

*Kruskal stress calculation*

---

**Description**

Calculates the stress as defined by Kruskal for 2 distance matrices

**Usage**

```
KruskalStress(InputDistances, OutputDistances)
```

**Arguments**

InputDistances Distance matrix of the original Data  
OutputDistances Distance matrix of the projected Data

**Details**

An short overview of different types of quality measures can be found in [Thrun, 2018, p.68, Fig. 6.3] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

A single numerical representing the Kruskal stress of the distance matrices.

**Author(s)**

Felix Pape

---

MDS

*Multidimensional Scaling (MDS)*

---

**Description**

Classical multidimensional scaling of a data matrix. Also known as principal coordinates analysis

**Usage**

```
MDS(DataOrDistances,method='euclidean',OutputDimension=2,PlotIt=FALSE,CIs)
```

**Arguments**

DataOrDistances	Numerical matrix defined as either Data, i.e., [1:n,1:d], nonsymmetric, and consists of n cases of d-dimensional data points with every case having d attributes, variables or features, or Distances, i.e.,[1:n,1:n], symmetric and consists of n cases, e.g., as <code>matrix(dist(Data,method))</code>
method	method specified by distance string: 'euclidean','cityblock=manhattan','cosine','chebychev','jaccard','m'
OutputDimension	Number of dimensions in the Outputspace, default=2
PlotIt	Default: FALSE, If TRUE: Plots the projection as a 2d visualization.
Cls	[1:n,1] Optional,: only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.

**Details**

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

ProjectedPoints	[1:n,OutputDimension], n by OutputDimension matrix containing coordinates of the Projection
Eigenvalues	the eigenvalues of <code>MDSvalues*MDSvalues'</code>
Stress	Shephard-Kruskal Stress

**Note**

A wrapper for `cmdscales`

You can use the standard `ShepardScatterPlot` or the better approach through the `ShepardDensityPlot` of the CRAN package `DataVisualizations`.

**Author(s)**

Michael Thrun

**Examples**

```
data('Hepta')
Data=Hepta$Data

Proj=MDS(Data)

## Not run:
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)
```

---

 NeRV

*Neighbor Retrieval Visualizer (NeRV)*


---

### Description

Projection is done by the neighbor retrieval visualizer (NeRV)

### Usage

```
NeRV(Data, lambda = 0.1, neighbors = 20, iterations = 10,
      cg_steps = 2, cg_steps_final = 40, randominit = T, OutputDimension = 2,
      PlotIt = FALSE, Cls)
```

### Arguments

Data	Numerical matrix of the Data to be projected, [1:n,1:d], nonsymmetric, and consists of n cases of d-dimensional data points with every case having d attributes, variables or features
lambda	Optional: Controls the trustworthiness-continuity tradeoff. Default = 0.1
neighbors	Optional: Set the number of nearest neighbours that each point should have. Should be positive. Default = 20
iterations	Optional: The number of iterations to perform. Default = 10
cg_steps	Optional: The number of conjugate gradient steps to perform per iteration in NeRV's optimization scheme. Default = 2
cg_steps_final	Optional: The number of conjugate gradient steps to perform on the final iteration in NeRV's optimization scheme. Default = 40
randominit	Optional: TRUE: Random Initialization (default), FALSE: PCA initialization
OutputDimension	Optional: Number of dimensions in the Outputspace, default=2
PlotIt	Optional: Should the projected points be plotted? Default: FALSE. Note: this is only usefull if OutputDimension = 2.
Cls	Optional: Vector containing the number of the class for each row in Data. This is only used to color the points according to their classes if PlotIt = T

### Details

Uses the NeRV projection with matrix Data and lambda. Lambda controls the trustworthiness-continuity tradeoff.

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

OutputDimension-dimensional matrix of projected points

**Note**

PCA initialization changes from the original C++ Sourcecode of <https://research.cs.aalto.fi/pml/software/dredviz/> to the R version of the projections package. Other changes are made only regarding data types of Rcpp in comparison to the original C++ Source code.

You can use the standard ShepardScatterPlot or the better approach through the ShepardDensityPlot of the CRAN package DataVisualizations.

**Author(s)**

Michael Thrun, Felix Pape

**References**

Jarkko Venna, Jaakko Peltonen, Kristian Nybo, Helena Aidos, and Samuel Kaski. Information Retrieval Perspective to Nonlinear Dimensionality Reduction for Data Visualization. *Journal of Machine Learning Research*, 11:451-490, 2010.

Jarkko Venna and Samuel Kaski. Nonlinear Dimensionality Reduction as Information Retrieval. In Marina Meila and Xiaotong Shen, editors, *Proceedings of AISTATS 2007, the 11th International Conference on Artificial Intelligence and Statistics*. Omnipress, 2007. *JMLR Workshop and Conference Proceedings, Volume 2: AISTATS 2007*.

**Examples**

```
data('Hepta')
Data=Hepta$Data
## Not run:
Proj=NeRV(Data)
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)
```

---

PCA

*Principal Component Analysis (PCA)*

---

**Description**

Performs a principal components analysis on the given data matrix `projection=SammonsMapping(Data)`

**Usage**

```
PCA(Data,OutputDimension=2,Scale=FALSE,Center=FALSE,PlotIt=FALSE,Cls)
```

**Arguments**

Data	numerical matrix of data: n cases in rows, d variables in columns
OutputDimension	Number of dimensions in the Outputspace, default=2
Scale	a logical value indicating whether the variables should be scaled to have unit variance before the analysis takes place. The default is FALSE for consistency with S, but in general scaling is advisable. Alternatively, a vector of length equal the number of columns of x can be supplied. The value is passed to scale.
Center	a logical value indicating whether the variables should be shifted to be zero centered. Alternately, a vector of length equal the number of columns of x can be supplied. The value is passed to scale
PlotIt	Default: FALSE, If TRUE: Plots the projection as a 2d visualization. OutputDimension>2: only the first two dimensions will be shown
Cls	[1:n,1] Optional,; only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.

**Details**

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

ProjectedPoints	[1:n,OutputDimension], n by OutputDimension matrix containing coordinates of the Projectio
Rotation	the matrix of variable loadings (i.e., a matrix whose columns contain the eigenvectors)
sDev	the standard deviations of the principal components (i.e., the square roots of the eigenvalues of the covariance/correlation matrix, though the calculation is actually done with the singular values of the data matrix)
TransformedData	matrix with PCA transformed Data
Center	the centering used, or FALSE
Scale	the scaling used, or FALSE

**Note**

A wrapper for [prcomp](#)

You can use the standard ShepardScatterPlot or the better approach through the ShepardDensityPlot of the CRAN package DataVisualizations.

**Author(s)**

Michael Thrun



**Examples**

```

data('Hepta')
Data=Hepta$Data

Proj=PCA(Data)

## Not run:
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)

```

---

PlotProjectedPoints    *Plot Projected Points*

---

**Description**

plots XY data colored by Cls with ggplot2

**Usage**

```

PlotProjectedPoints(Points,Cls,BMUorProjected=F,PlotLegend=FALSE,

xlab='X',ylab='Y',main="Projected Points",PointSize=2.5)

```

**Arguments**

Points	[1:n,1:2] xy cartesian coordinates of a projection
Cls	numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.
BMUorProjected	Default ==FALSE, If TRUE assuming BestMatches of ESOM instead of Projected Points
PlotLegend	...
xlab	Optional: Label of the x axis
ylab	Optional: Label of the y axis
main	Optional: title
PointSize	Optional: size of points

**Value**

ggobject of ggplot2

**Author(s)**

Michael Thrun

PolarSwarm

*Polar Swarm (Pswarm)***Description**

Swarm-based Projection method using game theory published in [Thrun/Ultsch, 2020].

**Usage**

```
PolarSwarm(DataOrDistances, method = "euclidean", PlotIt = FALSE, Cls)
```

**Arguments**

DataOrDistances

Numerical matrix defined as either

Data, i.e., [1:n,1:d], nonsymmetric, and consists of n cases of d-dimensional data points with every case having d attributes, variables or features,

or

Distances, i.e.,[1:n,1:n], symmetric and consists of n cases, e.g., `as.matrix(parallelDist::parallelDist(...))`

method

If Data is given the method to computing the distances can be specified here. Please see the documentation of package **parallelDist** for the types that are possible.

PlotIt

Default: FALSE, If TRUE: Plots the projection as a 2d visualization. OutputDimension>2: only the first two dimensions will be shown

Cls

Optional,; only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.

**Details**

By exploiting swarm intelligence and game theory no parameter have to be set.

**Value**

List of

ProjectedPoints

[1:n,2], n by 2 matrix containing coordinates of the Projection

ModelObject

output of [Pswarm](#)

**Author(s)**

Michael Thrun

**References**

[Thrun/Ultsch, 2020] Thrun, M. C., & Ultsch, A.: Swarm Intelligence for Self-Organized Clustering, Artificial intelligence, Vol. 290, pp. 103237, doi 10.1016/j.artint.2020.103237, 2020.

**See Also**[Pswarm](#)**Examples**

```

data('Hepta')
Data=Hepta$Data

Distances=as.matrix(dist(Data))
Proj=PolarSwarm(Data)
## Not run:
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)
## End(Not run)

```

---

 Projection2Bestmatches

*Projection to Bestmatches*


---

**Description**

Transformation of projected points to bestmatches defined by generalized Umatrix

**Usage**

```
Projection2Bestmatches(ProjectedPoints)
```

**Arguments**

ProjectedPoints  
 [1:n,1:2] n projected points in two-dimensional space.

**Details**

It is assumed that an unambiguous assignment between projected points and data points is given.

**Value**

Bestmatches	[1:n,1:2] Positions of GridConverted Projected Points, which can be used for the generalized Umatrix, to the predefined Grid by Lines and Columns. First Columns has the content of the Line No and second Column of the Column number.
LC	[1:2] vector if Line No. and ColumnNo. which defines the size of the grid of the generalized Umatrix

**Note**

Details of the equations used are written down in [Thrun, 2018, p. 47].

**Author(s)**

Michael Thrun

**References**

[Thrun, 2018] Thrun, M. C.: Projection Based Clustering through Self-Organization and Swarm Intelligence, doctoral dissertation 2017, Springer, Heidelberg, ISBN: 978-3-658-20539-3, [doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409), 2018.

**See Also**

[XYcoords2LinesColumns](#)

**Examples**

```
data('Hepta')
ProjList=MDS(Hepta$Data)
trafo=Projection2Bestmatches(ProjList$ProjectedPoints)
```

---

 ProjectionBasedClustering

*Automatic Projection-based Clustering (PBC) [Thrun/Ultsch, 2020]*

---

**Description**

Three steps are necessary for PBC. First, a projection method has to be chosen to generate projected points of high-dimensional data points. Second, the generalized U\*-matrix has to be applied to the projected points by using a simplified emergent self-organizing map (ESOM) algorithm which is an unsupervised neural network [Thrun, 2018]. The resulting generalized U-matrix can be visualized by the topographic map [Thrun et al., 2016]. Third, the clustering itself is built on top of the generalized U-matrix using the concept of the abstract U-Matrix and shortest graph paths using ShortestGraphPathsC.

**Usage**

```
ProjectionBasedClustering(k, DataOrDistances, BestMatches, LC,
  StructureType = TRUE, PlotIt = FALSE, method = "euclidean")
```

**Arguments**

**k** number of clusters, how many to you see in the 3d landscape?

**DataOrDistances** Numerical matrix that will be used for clustering with one DataPoint per row, defined as either as Data, i.e., [1:n,1:d], nonsymmetric, and consists of n cases of d-dimensional data points with every case having d attributes, variables or features,

	or Distances, i.e., [1:n, 1:n], symmetric and consists of n cases, e.g., as <code>matrix(dist(Data, method))</code>
BestMatches	[1:n, 1:2] Matrix with positions of Bestmatches=ProjectedPoints, one matrix line per data point
LC	grid size c(Lines, Columns)
StructureType	Optional, bool; =TRUE: compact structure of clusters assumed, =FALSE: connected structure of clusters assumed. For the two options vor Clusters, see [Thrun, 2017] or Handl et al. 2006
PlotIt	Optional, bool, Plots Dendrogramm
method	Optional, distance method used in <b>parallelDist</b> if Data given.

### Details

ProjectionBasedClustering is a flexible and robust clustering framework based on a chose projection method and projection method a parameter-free high-dimensional data visualization technique. The visualization combines projected points with a topographic map with hypsometric colors, defined by the generalized U-matrix (see package GeneralizedUmatrix function GeneralizedUmatrix).

The clustering method with no sensitive parameters is done in this function and the algorithm is introduced in detail in [Thrun/Ultsch, 2020]. The clustering can be verified by the visualization and vice versa. If you want to verify your clustering result externally, you can use Heatmap or SilhouettePlot of the CRAN package DataVisualizations.

If **parallelDist** is not installed, function automatically falls back to [dist](#).

### Value

Cls [1:n] vector with selected classes of the bestmatches. You can use `plotTopographicMap(Umatrix, Bestmatches, Cls)` for verification.

### Note

Often it is better to mark the outliers manually after the prozess of clustering; use in this case the visualization `plotTopographicMap` of the package GeneralizedUmatrix. If you would like to mark the outliers interactivly in the visualization use the `interactiveClustering` function.

### Author(s)

Michael Thrun

### References

[Thrun et al., 2016] Thrun, M. C., Lerch, F., Lötsch, J., & Ultsch, A.: Visualization and 3D Printing of Multivariate Data of Biomarkers, in Skala, V. (Ed.), International Conference in Central Europe on Computer Graphics, Visualization and Computer Vision (WSCG), Vol. 24, Plzen, <http://wscg.zcu.cz/wscg2016/short/A43-full.pdf>, 2016.

[Thrun/Ultsch, 2017] Thrun, M.C., Ultsch, A.: Projection based Clustering, Conf. Int. Federation of Classification Societies (IFCS), DOI:10.13140/RG.2.2.13124.53124, Tokyo, 2017.

[Thrun/Ultsch, 2020] Thrun, M. C., & Ultsch, A.: Using Projection based Clustering to Find Distance and Density based Clusters in High-Dimensional Data, Journal of Classification, Vol. 38(2), pp. 280-312, Springer, DOI: 10.1007/s00357-020-09373-2, 2020.

## Examples

```

data('Hepta')
#Step I: 2d projection
projectionpoints=NeRV(Hepta$Data)

#Step II (Optional): Computation of Generalized Umatrix
library(GeneralizedUmatrix)
visualization=GeneralizedUmatrix(Data = Hepta$Data,projectionpoints)
# Visualizuation of GeneralizedUmatrix
library(GeneralizedUmatrix)
TopviewTopographicMap(visualization$Umatrix,visualization$Bestmatches)
#or in 3D if rgl package exists
#plotTopographicMap(visualization$Umatrix,visualization$Bestmatches)

# Step III: Automatic Clustering
trafo=Projection2Bestmatches(projectionpoints)
# number of Cluster from dendrogram (PlotIt=T) or visualization above
Cls=ProjectionBasedClustering(k=7, Hepta$Data,

trafo$Bestmatches, trafo$LC,PlotIt=TRUE)

# Verification of Clustering
TopviewTopographicMap(visualization$Umatrix,visualization$Bestmatches,Cls)
#or in 3D if rgl package exists
#plotTopographicMap(visualization$Umatrix,visualization$Bestmatches,Cls)

```

---

ProjectionPursuit

*Projection Pursuit*

---

## Description

In the absence of a generative model for the data the algorithm can be used to find the projection pursuit directions. Projection pursuit is a technique for finding 'interesting' directions in multidimensional datasets

## Usage

```

ProjectionPursuit(Data,OutputDimension=2,Indexfunction="logcosh",

Alpha=1,Iterations=200,PlotIt=FALSE,Cls)

```

**Arguments**

Data	array of data: n cases in rows, d variables in columns, matrix is not symmetric or distance matrix, in this case matrix has to be symmetric
OutputDimension	Number of dimensions in the Outputspace, default=2
Indexfunction	Criterion for Minimization: default: 'logcosh' $G(u)=1/a*\log \cosh(a*u)$ (ICA) 'exp': $G(u)=-\exp(u^2/2)$ 'kernel' $1/(1* \pi )*\exp(r/2)$
Alpha	constant with $1\leq\alpha\leq 2$ used in approximation to neg-entropy when fun == "logcosh"
Iterations	maximum number of iterations to perform.
PlotIt	Default: FALSE, If TRUE: Plots the projection as a 2d visualization. OutputDimension>2: only the first two dimensions will be shown
Cls	[1:n,1] Optional,: only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.

**Details**

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

ProjectedPoints  
[1:n,OutputDimension], n by OutputDimension matrix containing coordinates of the Projectio

**Note**

You can use the standard ShepardScatterPlot or the better approach through the ShepardDensityPlot of the CRAN package DataVisualizations.

**Author(s)**

Michael Thrun

---

SammonsMapping

*Sammons Mapping*

---

**Description**

Improved MDS through a normalization of the Input space

**Usage**

```
SammonsMapping(DataOrDistances,method='euclidean',OutputDimension=2,PlotIt=FALSE,Cls)
```

**Arguments**

DataOrDistances

Numerical matrix defined as either

Data, i.e., [1:n,1:d], nonsymmetric, and consists of n cases of d-dimensional data points with every case having d attributes, variables or features,

or

Distances, i.e.,[1:n,1:n], symmetric and consists of n cases, e.g., as `matrix(dist(Data,method))`

method

method specified by distance string: 'euclidean','cityblock=manhattan','cosine','chebychev','jaccard','m

OutputDimension

Number of dimensions in the Outputspace, default=2

PlotIt

Default: FALSE, If TRUE: Plots the projection as a 2d visualization.

Cls

[1:n,1] Optional,; only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.

**Details**

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1] ([doi:10.1007/9783658205409](https://doi.org/10.1007/9783658205409)).

**Value**

ProjectedPoints

[1:n,OutputDimension], n by OutputDimension matrix containing coordinates of the Projectio

Stress

Shephard-Kruskal Stress

**Note**

A wrapper for [sammon](#)

You can use the standard ShepardScatterPlot or the better approach through the ShepardDensityPlot of the CRAN package DataVisualizations.

**Author(s)**

Michael Thrun

**Examples**

```
data('Hepta')
Data=Hepta$Data
```

```
Proj=SammonsMapping(Data)
```



```
## Not run:
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)
```

---

ShortestGraphPathsC     *Shortest GraphPaths = geodesic distances*

---

### Description

Dijkstra's SSSP (Single source shortest path) algorithm, from all points to all points

### Usage

```
ShortestGraphPathsC(Adj, Cost)
```

### Arguments

Adj                    [1:n,1:n] 0/1 adjascency matrix, e.g. from delaunay graph or gabriel graph  
 Cost                   [1:n,1:n] matrix, distances between n points (normally euclidean)

### Details

Vertices are the points, edges have the costs defined by weights (normally a distance). The algorithm runs in runs in  $O(n^2 \log(V))$ , see also [Jungnickel, 2013, p. 87]. Further details can be found in [Jungnickel, 2013, p. 83-87].

### Value

ShortestPaths[1:n,1:n] vector, shortest paths (geodesic) to all other vertices including the source vertice itself from al vertices to all vertices, stored as a matrix

### Note

require C++11 standard (set flag in Compiler, if not set automatically)

### Author(s)

Michael Thrun

### References

- [Dijkstra, 1959] Dijkstra, E. W.: A note on two problems in connexion with graphs, Numerische mathematik, Vol. 1(1), pp. 269-271. 1959.
- [Jungnickel, 2013] Jungnickel, D.: Graphs, networks and algorithms, (4th ed ed. Vol. 5), Berlin, Heidelberg, Germany, Springer, ISBN: 978-3-642-32278-5, 2013.
- [Thrun/Ultsch, 2017] Thrun, M.C., Ultsch, A.: Projection based Clustering, Conf. Int. Federation of Classification Societies (IFCS),DOI:10.13140/RG.2.2.13124.53124, Tokyo, 2017.

**See Also**[DijkstraSSSP](#)


---

tSNE	<i>T-distributed Stochastic Neighbor Embedding (t-SNE)</i>
------	--

---

**Description**

T-distributed Stochastic Neighbor Embedding `res = tSNE(Data, KNN=30, OutputDimension=2)`

**Usage**

```
tSNE(DataOrDistances, k, OutputDimension=2, Algorithm='tsne_cpp',
      method="euclidean", Whitening=FALSE, Iterations=1000, PlotIt=FALSE, CIs, num_threads=1, ...)
```

**Arguments**

DataOrDistances	Numerical matrix defined as either Data, i.e., [1:n,1:d], nonsymmetric, and consists of n cases of d-dimensional data points with every case having d attributes, variables or features, or Distances, i.e., [1:n,1:n], symmetric and consists of n cases, e.g., as <code>matrix(dist(Data, method))</code>
k	number of k nearest neighbors=number of effective nearest neighbors("perplexity"); Important parameter. If not given, settings of packages of t-SNE will be used depending Algorithm
OutputDimension	Number of dimensions in the Outputspace, default=2
Algorithm	'tsne_cpp': T-Distributed Stochastic Neighbor Embedding using a Barnes-HutImplementation in C++ of <b>Rtsne</b> . Requires Version >= 0.15 of <b>Rtsne</b> for multicore parallelisation. 'tsne_opt_cpp': T-Distributed Stochastic Neighbor Embedding with automated optimized parameters using a Barnes-HutImplementation in C++ of [Ulyanov, 2016]. 'tsne_r': pure R implementation of the t-SNE algorithm of of <b>tsne</b>
method	method specified by distance string: 'euclidean', 'cityblock=manhattan', 'cosine', 'chebychev', 'jaccard', 'm
Whitening	A boolean value indicating whether the matrix data should be whitened (tsne_r) or if pca should be used priorly (tsne_cpp)
Iterations	maximum number of iterations to perform.
PlotIt	Default: FALSE, If TRUE: Plots the projection as a 2d visualization. OutputDimension>2: only the first two dimensions will be shown

Cls	[1:n,1] Optional,; only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.
num_threads	Number of threads for parallel computation, only usable for Algorithm='tsne_cpp' or 'tsne_opt_cpp'
...	Further arguments passed on to either 'Rtsne' or 'tsne'

### Details

An short overview of different types of projection methods can be found in [Thrun, 2018, p.42, Fig. 4.1], doi:[10.1007/9783658205409](https://doi.org/10.1007/9783658205409).

### Value

List of	
ProjectedPoints	[1:n,OutputDimension], n by OutputDimension matrix containing coordinates of the Projection
ModelObject	NULL for tsne_r, further information if tsne_cpp is selected

### Note

A wrapper for [Rtsne](#) (Algorithm='tsne\_cpp'),  
[Multicore-opt-tSNE](#) (Algorithm='tsne\_opt\_cpp'),  
 or for [tsne](#) (Algorithm='tsne\_r')

You can use the standard ShepardScatterPlot or the better approach through the ShepardDensityPlot of the CRAN package DataVisualizations.

### Author(s)

Michael Thrun, Luca Brinkmann

### References

- Anna C. Belkina, Christopher O. Ciccolella, Rina Anno, Josef Spidlen, Richard Halpert, Jennifer Snyder-Cappione: Automated optimal parameters for T-distributed stochastic neighbor embedding improve visualization and allow analysis of large datasets, bioRxiv 451690, doi: <https://doi.org/10.1101/451690>, 2018.
- L.J.P van der Maaten: Accelerating t-SNE using tree-based algorithms, Journal of Machine Learning Research 15.1:3221-3245, 2014.
- Ulyanov, Dmitry: Multicore-TSNE, GitHub repository URL <https://github.com/DmitryUlyanov/Multicore-TSNE>, 2016.

**Examples**

```

data('Hepta')
Data=Hepta$Data

## Not run:
Proj=tSNE(Data,k=7)

PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)

```

---

UniformManifoldApproximationProjection  
*Uniform Manifold Approximation and Projection*

---

**Description**

Uniform manifold approximation and projection is a technique for dimension reduction. The algorithm was described by [McInnes et al., 2018].

**Usage**

```

UniformManifoldApproximationProjection(DataOrDistances, k,
Epochs,OutputDimension=2,Algorithm='umap_pkg',PlotIt=FALSE,Cls,...)

```

**Arguments**

DataOrDistances	Numerical matrix defined as either Data, i.e., [1:n,1:d], nonsymmetric, and consists of n cases of d-dimensional data points with every case having d attributes, variables or features, or Distances, i.e.,[1:n,1:n], symmetric and consists of n cases, e.g., as.matrix(dist(Data,method))
k	number of k nearest neighbors, Important parameter, if not given, settings of package <b>umap</b> will be used, default of package <b>umap</b> is currently 15
Epochs	Number of eppochs (scalar), i.e, training length, default of package <b>umap</b> is currently 200
OutputDimension	Number of dimensions in the Outputspace, default=2
Algorithm	"umap_pkg": provides an interface for two implementations. One is written from scratch other one requires python <b>umap</b> "uwot_pkg": complete re-implementation in R (and C++, via the 'Rcpp' package) of <b>uwot</b>

PlotIt	Default: FALSE, If TRUE: Plots the projection as a 2d visualization. OutputDimension>2: only the first two dimensions will be shown
Cls	Optional,; only relevant if PlotIt=TRUE. Numeric vector, given Classification in numbers: every element is the cluster number of a certain corresponding element of data.
...	one of the other 21 parameters that can be specified, please see <a href="#">umap.defaults</a> of package <b>umap</b> for details or parameters to be set in package <b>uwot</b> depending on the choice of Algorithm.

### Details

To the knowledge of the author of this function no peer-reviewed publication of the method exists. Use with great care.

### Value

List of ProjectedPoints	[1:n,OutputDimension], n by OutputDimension matrix containing coordinates of the Projection
ModelObject	output of <a href="#">umap</a> or of package <b>uwot</b> depending on Algorithm
Setting	specific settings used in UniformManifoldApproximationProjection

### Note

Uniform Manifold Approximation and Projection and U-matrix [Ultsch/Siemon, 1990] are both sometimes abbreviated with Umap. Hence the abbreviation is omitted here.

### Author(s)

Michael Thrun

### References

[McInnes et al., 2018] McInnes, L., Healy, J., & Melville, J.: Umap: Uniform manifold approximation and projection for dimension reduction, arXiv preprint arXiv:1802.03426, 2018.

[Ultsch/Siemon, 1990] Ultsch, A., & Siemon, H. P.: Kohonen's Self Organizing Feature Maps for Exploratory Data Analysis, International Neural Network Conference, pp. 305-308, Kluwer Academic Press, Paris, France, 1990.

### See Also

[umap](#) of **umap**

[umap](#) of **uwot**

**Examples**

```
data('Hepta')
Data=Hepta$Data

Proj=UniformManifoldApproximationProjection(Data)

## Not run:
PlotProjectedPoints(Proj$ProjectedPoints,Hepta$Cls)

## End(Not run)
```

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