# Package 'networkscaleup'

February 25, 2024

Version 0.1-2
Description Provides a variety of Network Scale-up Models for researchers to analyze Aggregated Relational Data, mostly through the use of Stan. In this version, the package implements models from Laga, I., Bao, L., and Niu, X (2021) <arXiv:2109.10204>, Zheng, T., Salganik, M. J., and Gelman, A. (2006) <doi:10.1198/016214505000001168>, Killworth, P. D., Johnsen, E. C., McCarty, C., Shelley, G. A., and Bernard, H. R. (1998) <doi:10.1016/S0378-8733(96)00305-X>, and Killworth, P. D., McCarty, C., Bernard, H. R., Shelley, G. A., and Johnsen, E. C. (1998) <doi:10.1177/0193841X9802200205>.
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Suggests rmarkdown, knitr

VignetteBuilder knitr

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**NeedsCompilation** yes

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networkscaleup-package

The 'networkscaleup' package.

## **Description**

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Provides a variety of Network Scale-up Models for researchers to analyze Aggregated Relational Data, mostly through the use of Stan.

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#### References

Stan Development Team (2021). RStan: the R interface to Stan. R package version 2.21.3. https://mc-stan.org

Laga, I., Bao, L., and Niu, X (2021). A Correlated Network Scaleup Model: Finding the Connection Between Subpopulations

Zheng, T., Salganik, M. J., and Gelman, A. (2006). How many people do you know in prison, *Journal of the American Statistical Association*, **101:474**, 409–423

Killworth, P. D., Johnsen, E. C., McCarty, C., Shelley, G. A., and Bernard, H. R. (1998). A Social Network Approach to Estimating Seroprevalence in the United States, *Social Networks*, **20**, 23–50

Killworth, P. D., McCarty, C., Bernard, H. R., Shelley, G. A., and Johnsen, E. C. (1998). Estimation of Seroprevalence, Rape and Homelessness in the United States Using a Social Network Approach, *Evaluation Review*, **22**, 289–308

correlatedStan

Fit ARD using the uncorrelated or correlated model in Stan This function fits the ARD using either the uncorrelated or correlated model in Laga et al. (2021) in Stan. The population size estimates and degrees are scaled using a post-hoc procedure.

# **Description**

Fit ARD using the uncorrelated or correlated model in Stan This function fits the ARD using either the uncorrelated or correlated model in Laga et al. (2021) in Stan. The population size estimates and degrees are scaled using a post-hoc procedure.

## Usage

```
correlatedStan(
  ard,
  known_sizes = NULL,
  known_ind = NULL,
  N = NULL
  model = c("correlated", "uncorrelated"),
  scaling = c("all", "overdispersed", "weighted", "weighted_sq"),
  x = NULL,
  z_global = NULL,
  z_{subpop} = NULL,
  G1_{ind} = NULL
  G2_{ind} = NULL,
 B2_{ind} = NULL,
  chains = 3,
  cores = 1,
 warmup = 1000,
  iter = 1500,
  thin = 1,
  return_fit = FALSE,
)
```

## **Arguments**

ard	The 'n_i x n_k' matrix of non-negative ARD integer responses, where the ' $(i,k)$ th' element corresponds to the number of people that respondent 'i' knows in subpopulation 'k'.
known_sizes	The known subpopulation sizes corresponding to a subset of the columns of ard.
known_ind	The indices that correspond to the columns of ard with known_sizes. By default, the function assumes the first $n_k$ nown columns, where $n_k$ nown corresponds to the number of known_sizes.

N The known total population size.

model	A character vector denoting which of the two models should be fit, either 'uncorrelated' or 'correlated'. More details of these models are provided below. The function decides which covariate model is needed based on the covariates provided below.
scaling	An optional character vector providing the name of scaling procedure should be performed in order to transform estimates to degrees and subpopulation sizes. If 'NULL', the parameters will be returned unscaled. Alternatively, scaling may be performed independently using the scaling function. Scaling options are 'NULL', 'overdispersed', 'all', 'weighted', or 'weighted_sq' ('weighted' and 'weighted_sq' are only available if 'model = "correlated"'. Further details are provided in the Details section.
X	A matrix with dimensions 'n_i x n_unknown', where 'n_unknown' refers to the number of unknown subpopulation sizes. In the language of Teo et al. (2019), these represent the individual's perception of each hidden population.
z_global	A matrix with dimensions 'n_i x p_global', where 'p_global' is the number of demographic covariates used. This matrix represents the demographic information about the respondents in order to capture the barrier effects.
z_subpop	A matrix with dimensions 'n_i x p_subpop', where 'p_subpop' is the number of demographic covariates used. This matrix represents the demographic information about the respondents in order to capture the barrier effects.
G1_ind	A vector of indices denoting the columns of 'ard' that correspond to the primary scaling groups, i.e. the collection of rare girls' names in Zheng, Salganik, and Gelman (2006). By default, all known_sizes are used. If G2_ind and B2_ind are not provided, 'C = C_1', so only G1_ind are used. If G1_ind is not provided, no scaling is performed.
G2_ind	A vector of indices denoting the columns of 'ard' that correspond to the subpopulations that belong to the first secondary scaling groups, i.e. the collection of somewhat popular girls' names.
B2_ind	A vector of indices denoting the columns of 'ard' that correspond to the subpopulations that belong to the second secondary scaling groups, i.e. the collection of somewhat popular boys' names.
chains	A positive integer specifying the number of Markov chains.
cores	A positive integer specifying the number of cores to use to run the Markov chains in parallel.
warmup	A positive integer specifying the total number of samples for each chain (including warmup). Matches the usage in stan.
iter	A positive integer specifying the number of warmup samples for each chain. Matches the usage in stan.
thin	A positive integer specifying the interval for saving posterior samples. Default value is 1 (i.e. no thinning).
return_fit	A logical indicating whether the fitted 'stanfit' object should be return. Defaults to 'FALSE'.
	Additional arguments to be passed to stan.

#### **Details**

This function currently fits a variety of models proposed in Laga et al. (2022+). The user may provide any combination of 'x', 'z\_global', and 'z\_subpop'. Additionally, the user may choose to fit a uncorrelated version of the model, where the correlation matrix is equal to the identity matrix.

The 'scaling' options are described below:

**NULL** No scaling is performed

**overdispersed** The scaling procedure outlined in Zheng et al. (2006) is performed. In this case, at least 'Pg1\_ind' must be provided. See overdispersedStan for more details.

all All subpopulations with known sizes are used to scale the parameters, using a modified scaling procedure that standardizes the sizes so each population is weighted equally. Additional details are provided in Laga et al. (2022+).

weighted All subpopulations with known sizes are weighted according their correlation with the unknown subpopulation size. Additional details are provided in Laga et al. (2022+)

weighted\_sq Same as 'weighted', except the weights are squared, providing more relative weight to subpopulations with higher correlation.

#### Value

Either the full fitted Stan model if return\_fit = TRUE, else a named list with the estimated parameters extracted using extract (the default). The estimated parameters are named as follows (if estimated in the corresponding model), with additional descriptions as needed:

**delta** Raw delta parameters

sigma\_delta Standard deviation of delta

rho Log prevalence, if scaled, else raw rho parameters

mu\_rho Mean of rho

sigma\_rho Standard deviation of rho

alpha Slope parameters corresponding to z

beta\_global Slope parameters corresponding to x\_global

**beta\_subpop** Slope parameters corresponding to x\_subpop

tau N Standard deviation of random effects b

**Corr** Correlation matrix, if 'Correlation = TRUE'

If scaled, the following additional parameters are included:

log\_degrees Scaled log degrees

degree Scaled degrees

log\_prevalences Scaled log prevalences

sizes Subpopulation size estimates

#### References

Laga, I., Bao, L., and Niu, X (2021). A Correlated Network Scaleup Model: Finding the Connection Between Subpopulations

## **Examples**

```
## Not run:
data(example_data)
x = example_data$x
z_global = example_data$z[,1:2]
z_subpop = example_data$z[,3:4]
basic_corr_est = correlatedStan(example_data$ard,
     known_sizes = example_data$subpop_sizes[c(1, 2, 4)],
     known_ind = c(1, 2, 4),
    N = example_data N,
    model = "correlated",
    scaling = "weighted",
    chains = 1,
    cores = 1,
     warmup = 50,
     iter = 100)
cov_uncorr_est = correlatedStan(example_data$ard,
     known_sizes = example_data$subpop_sizes[c(1, 2, 4)],
     known_ind = c(1, 2, 4),
    N = example_data$N,
    model = "uncorrelated",
    scaling = "all",
    x = x,
    z_global = z_global,
    z_{subpop} = z_{subpop}
    chains = 1,
    cores = 1,
    warmup = 50,
    iter = 100)
cov_corr_est = correlatedStan(example_data$ard,
     known_sizes = example_data$subpop_sizes[c(1, 2, 4)],
     known_ind = c(1, 2, 4),
    N = example_data$N,
    model = "correlated",
    scaling = "all",
    x = x
    z_{subpop} = z_{subpop}
    chains = 1,
    cores = 1,
     warmup = 50,
     iter = 100)
# Compare size estimates
round(data.frame(true = example_data$subpop_sizes,
     corr_basic = colMeans(basic_corr_est$sizes),
     uncorr_x_zsubpop_zglobal = colMeans(cov_uncorr_est$sizes),
     corr_x_zsubpop = colMeans(cov_corr_est$sizes)))
```

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```
# Look at z slope parameters
colMeans(cov_uncorr_est$beta_global)
colMeans(cov_corr_est$beta_subpop)
colMeans(cov_uncorr_est$beta_subpop)

# Look at x slope parameters
colMeans(cov_uncorr_est$alpha)
colMeans(cov_corr_est$alpha)
## End(Not run)
```

example\_data

Simulated ARD data set with z and x.

# **Description**

A simulated data set to demonstrate and test the NSUM methods. The data was simulated from the basic Killworth Binomial model.

# Usage

example\_data

#### Format

A named list for an ARD survey from 100 respondents about 5 subpopulations.

ard A '100 x 5' matrix with integer valued respondents

x A '100 x 5' matrix with simulated answers from a 1-5 Likert scale

z A '100 x 4' matrix with answers for each respondents about 4 demographic questions

N An integer specifying the total population size

subpop\_size A vector with the 5 true subpopulation sizes

degrees A vector with the 100 true respondent degrees

killworth

Fit Killworth models to ARD. This function estimates the degrees and population sizes using the plug-in MLE and MLE estimator.

# Description

Fit Killworth models to ARD. This function estimates the degrees and population sizes using the plug-in MLE and MLE estimator.

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## Usage

```
killworth(
  ard,
  known_sizes = NULL,
  known_ind = 1:length(known_sizes),
  N = NULL,
  model = c("MLE", "PIMLE")
)
```

## **Arguments**

ard The 'n\_i x n\_k' matrix of non-negative ARD integer responses, where the '(i,k)th'

element corresponds to the number of people that respondent 'i' knows in sub-

population 'k'.

known\_sizes The known subpopulation sizes corresponding to a subset of the columns of ard.

known\_ind The indices that correspond to the columns of ard with known\_sizes. By default,

the function assumes the first n\_known columns, where n\_known corresponds to

the number of known\_sizes.

N The known total population size.

model A character string corresponding to either the plug-in MLE (PIMLE) or the MLE

(MLE). The function assumes MLE by default.

#### Value

A named list with the estimated degrees and sizes.

### References

Killworth, P. D., Johnsen, E. C., McCarty, C., Shelley, G. A., and Bernard, H. R. (1998). A Social Network Approach to Estimating Seroprevalence in the United States, *Social Networks*, **20**, 23–50

Killworth, P. D., McCarty, C., Bernard, H. R., Shelley, G. A., and Johnsen, E. C. (1998). Estimation of Seroprevalence, Rape and Homelessness in the United States Using a Social Network Approach, *Evaluation Review*, **22**, 289–308

Laga, I., Bao, L., and Niu, X. (2021). Thirty Years of the Network Scale-up Method, *Journal of the American Statistical Association*, **116:535**, 1548–1559

#### **Examples**

```
# Analyze an example ard data set using the killworth function
data(example_data)

ard = example_data$ard
subpop_sizes = example_data$subpop_sizes
N = example_data$N

mle.est = killworth(ard,
known_sizes = subpop_sizes[c(1, 2, 4)],
known_ind = c(1, 2, 4),
```

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```
N = N, model = "MLE")
pimle.est = killworth(ard,
known_sizes = subpop_sizes[c(1, 2, 4)],
known_ind = c(1, 2, 4),
N = N, model = "PIMLE")
## Compare estimates with the truth
plot(mle.est$degrees, example_data$degrees)
data.frame(true = subpop_sizes[c(3, 5)],
mle = mle.est$sizes,
pimle = pimle.est$sizes)
```

overdispersed

Fit Overdispersed model to ARD (Gibbs-Metropolis)

## **Description**

This function fits the ARD using the Overdispersed model using the original Gibbs-Metropolis Algorithm provided in Zheng, Salganik, and Gelman (2006). The population size estimates and degrees are scaled using a post-hoc procedure. For the Stan implementation, see overdispersedStan.

## Usage

```
overdispersed(
  ard,
  known_sizes = NULL,
  known_ind = NULL,
 G1_{ind} = NULL,
 G2_{ind} = NULL,
 B2_{ind} = NULL,
 N = NULL
 warmup = 1000,
  iter = 1500,
  refresh = NULL,
  thin = 1,
  verbose = FALSE,
  alpha_tune = 0.4,
 beta_tune = 0.2,
 omega_tune = 0.2,
  init = "MLE"
)
```

#### **Arguments**

ard

The 'n\_i x n\_k' matrix of non-negative ARD integer responses, where the '(i,k)th' element corresponds to the number of people that respondent 'i' knows in subpopulation 'k'.

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known\_sizes The known subpopulation sizes corresponding to a subset of the columns of ard. known\_ind The indices that correspond to the columns of ard with known\_sizes. By default, the function assumes the first n\_known columns, where n\_known corresponds to the number of known\_sizes. G1\_ind A vector of indices denoting the columns of 'ard' that correspond to the primary scaling groups, i.e. the collection of rare girls' names in Zheng, Salganik, and Gelman (2006). By default, all known\_sizes are used. If G2\_ind and B2\_ind are not provided, ' $C = C_1$ ', so only G1\_ind are used. If G1\_ind is not provided, no scaling is performed. G2\_ind A vector of indices denoting the columns of 'ard' that correspond to the subpopulations that belong to the first secondary scaling groups, i.e. the collection of somewhat popular girls' names. B2\_ind A vector of indices denoting the columns of 'ard' that correspond to the subpopulations that belong to the second secondary scaling groups, i.e. the collection of somewhat popular boys' names. Ν The known total population size. warmup A positive integer specifying the number of warmup samples. iter A positive integer specifying the total number of samples (including warmup). refresh An integer specifying how often the progress of the sampling should be reported. By default, resorts to every 10 verbose = FALSE. thin A positive integer specifying the interval for saving posterior samples. Default value is 1 (i.e. no thinning). verbose Logical value, specifying whether sampling progress should be reported. A positive numeric indicating the standard deviation used as the jumping scale alpha\_tune in the Metropolis step for alpha. Defaults to 0.4, which has worked well for other ARD datasets. A positive numeric indicating the standard deviation used as the jumping scale beta\_tune in the Metropolis step for beta Defaults to 0.2, which has worked well for other ARD datasets. A positive numeric indicating the standard deviation used as the jumping scale omega\_tune in the Metropolis step for omega Defaults to 0.2, which has worked well for other ARD datasets. init A named list with names corresponding to the first-level model parameters, name 'alpha', 'beta', and 'omega'. By default the 'alpha' and 'beta' parameters are initialized at the values corresponding to the Killworth MLE estimates (for the missing 'beta'), with all 'omega' set to 20. Alternatively, init = 'random' simulates 'alpha' and 'beta' from a normal random variable with mean 0 and standard deviation 1. By default, init = 'MLE' initializes values at the Killworth et al. (1998b) MLE estimates for the degrees and sizes and simulates the other parameters.

#### **Details**

This function fits the overdispersed NSUM model using the Metropolis-Gibbs sampler provided in Zheng et al. (2006).

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#### Value

A named list with the estimated posterior samples. The estimated parameters are named as follows, with additional descriptions as needed:

alphas Log degree, if scaled, else raw alpha parameters
betas Log prevalence, if scaled, else raw beta parameters
inv\_omegas Inverse of overdispersion parameters
sigma\_alpha Standard deviation of alphas
mu\_beta Mean of betas
sigma\_beta Standard deviation of betas
omegas Overdispersion parameters

If scaled, the following additional parameters are included:

mu\_alpha Mean of log degreesdegrees Degree estimatessizes Subpopulation size estimates

#### References

Zheng, T., Salganik, M. J., and Gelman, A. (2006). How many people do you know in prison, *Journal of the American Statistical Association*, **101:474**, 409–423

# Examples

```
# Analyze an example ard data set using Zheng et al. (2006) models
# Note that in practice, both warmup and iter should be much higher
data(example_data)
ard = example_data$ard
subpop_sizes = example_data$subpop_sizes
known_ind = c(1, 2, 4)
N = example_data$N
overdisp.est = overdispersed(ard,
known_sizes = subpop_sizes[known_ind],
known_ind = known_ind,
G1_{ind} = 1,
G2_{ind} = 2,
B2_{ind} = 4,
N = N,
warmup = 50,
iter = 100)
# Compare size estimates
data.frame(true = subpop_sizes,
basic = colMeans(overdisp.est$sizes))
# Compare degree estimates
```

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```
plot(example_data$degrees, colMeans(overdisp.est$degrees))
# Look at overdispersion parameter
colMeans(overdisp.est$omegas)
```

overdispersedStan

Fit ARD using the Overdispersed model in Stan

#### **Description**

This function fits the ARD using the Overdispersed model in Stan. The population size estimates and degrees are scaled using a post-hoc procedure. For the Gibbs-Metropolis algorithm implementation, see overdispersed.

# Usage

```
overdispersedStan(
  ard,
  known_sizes = NULL,
  known_ind = NULL,
  G1_ind = NULL,
  G2_ind = NULL,
  B2_ind = NULL,
  N = NULL,
  chains = 3,
  cores = 1,
  warmup = 1000,
  iter = 1500,
  thin = 1,
  return_fit = FALSE,
  ...
)
```

## **Arguments**

ard

The 'n\_i x n\_k' matrix of non-negative ARD integer responses, where the '(i,k)th' element corresponds to the number of people that respondent 'i' knows in subpopulation 'k'.

known\_sizes

The known subpopulation sizes corresponding to a subset of the columns of ard.

known\_ind

The indices that correspond to the columns of ard with known\_sizes. By default, the function assumes the first n\_known columns, where n\_known corresponds to the number of known\_sizes.

G1\_ind

A vector of indices denoting the columns of 'ard' that correspond to the primary scaling groups, i.e. the collection of rare girls' names in Zheng, Salganik, and Gelman (2006). By default, all known\_sizes are used. If G2\_ind and B2\_ind are not provided, ' $C = C_1$ ', so only G1\_ind are used. If G1\_ind is not provided, no scaling is performed.

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G2_ind	A vector of indices denoting the columns of 'ard' that correspond to the subpopulations that belong to the first secondary scaling groups, i.e. the collection of somewhat popular girls' names.
B2_ind	A vector of indices denoting the columns of 'ard' that correspond to the subpopulations that belong to the second secondary scaling groups, i.e. the collection of somewhat popular boys' names.
N	The known total population size.
chains	A positive integer specifying the number of Markov chains.
cores	A positive integer specifying the number of cores to use to run the Markov chains in parallel.
warmup	A positive integer specifying the total number of samples for each chain (including warmup). Matches the usage in stan.
iter	A positive integer specifying the number of warmup samples for each chain. Matches the usage in stan.
thin	A positive integer specifying the interval for saving posterior samples. Default value is 1 (i.e. no thinning).
return_fit	A logical indicating whether the fitted Stan model should be returned instead of the rstan::extracted and scaled parameters. This is FALSE by default.
	Additional arguments to be passed to stan.

#### **Details**

This function fits the overdispersed NSUM model using the Gibbs-Metropolis algorithm provided in Zheng et al. (2006).

## Value

Either the full fitted Stan model if return\_fit = TRUE, else a named list with the estimated parameters extracted using extract (the default). The estimated parameters are named as follows, with additional descriptions as needed:

alphas Log degree, if 'scaling = TRUE', else raw alpha parameters
 betas Log prevalence, if 'scaling = TRUE', else raw beta parameters
 inv\_omegas Inverse of overdispersion parameters
 sigma\_alpha Standard deviation of alphas
 mu\_beta Mean of betas
 sigma\_beta Standard deviation of betas
 omegas Overdispersion parameters

If 'scaling = TRUE', the following additional parameters are included:

mu\_alpha Mean of log degreesdegrees Degree estimatessizes Subpopulation size estimates

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#### References

Zheng, T., Salganik, M. J., and Gelman, A. (2006). How many people do you know in prison, *Journal of the American Statistical Association*, **101:474**, 409–423

#### **Examples**

```
# Analyze an example ard data set using Zheng et al. (2006) models
# Note that in practice, both warmup and iter should be much higher
## Not run:
data(example_data)
ard = example_data$ard
subpop_sizes = example_data$subpop_sizes
known_ind = c(1, 2, 4)
N = example_data$N
overdisp.est = overdispersedStan(ard,
known_sizes = subpop_sizes[known_ind],
known_ind = known_ind,
G1_{ind} = 1,
G2_{ind} = 2,
B2_ind = 4,
N = N,
chains = 1,
cores = 1,
warmup = 250,
iter = 500)
# Compare size estimates
round(data.frame(true = subpop_sizes,
basic = colMeans(overdisp.est$sizes)))
# Compare degree estimates
plot(example_data$degrees, colMeans(overdisp.est$degrees))
# Look at overdispersion parameter
colMeans(overdisp.est$omegas)
## End(Not run)
```

scaling

Scale raw log degree and log prevalence estimates

# Description

This function scales estimates from either the overdispersed model or from the correlated models. Several scaling options are available.

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#### Usage

```
scaling(
  log_degrees,
  log_prevalences,
  scaling = c("all", "overdispersed", "weighted", "weighted_sq"),
  known_sizes = NULL,
  known_ind = NULL,
  Correlation = NULL,
  G1_{ind} = NULL,
  G2_{ind} = NULL,
 B2_{ind} = NULL,
 N = NULL
)
```

#### **Arguments**

log\_degrees

The matrix of estimated raw log degrees from either the overdispersed or correlated models.

log\_prevalences

The matrix of estimates raw log prevalences from either the overdispersed or

correlated models.

scaling

An character vector providing the name of scaling procedure should be performed in order to transform estimates to degrees and subpopulation sizes. Scaling options are 'overdispersed', 'all' (the default), 'weighted', or 'weighted\_sq' ('weighted' and 'weighted\_sq' are only available if 'Correlation' is provided. Further details are provided in the Details section.

known\_sizes

The known subpopulation sizes corresponding to a subset of the columns of ard.

known\_ind

The indices that correspond to the columns of ard with known sizes. By default, the function assumes the first n\_known columns, where n\_known corresponds to the number of known\_sizes.

Correlation

The estimated correlation matrix used to calculate scaling weights. Required if 'scaling = weighted' or 'scaling = weighted\_sq'.

G1\_ind

If 'scaling = overdispersed', a vector of indices corresponding to the subpopulations that belong to the primary scaling groups, i.e. the collection of rare girls' names in Zheng, Salganik, and Gelman (2006). By default, all known\_sizes are used. If G2\_ind and B2\_ind are not provided, 'C = C\_1', so only G1\_ind are used. If G1\_ind is not provided, no scaling is performed.

G2\_ind

If 'scaling = overdispersed', a vector of indices corresponding to the subpopulations that belong to the first secondary scaling groups, i.e. the collection of somewhat popular girls' names.

B2\_ind

If 'scaling = overdispersed', a vector of indices corresponding to the subpopulations that belong to the second secondary scaling groups, i.e. the collection of somewhat popular boys' names.

Ν

The known total population size.

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#### **Details**

The 'scaling' options are described below:

**NULL** No scaling is performed

- **overdispersed** The scaling procedure outlined in Zheng et al. (2006) is performed. In this case, at least 'Pg1\_ind' must be provided. See overdispersedStan for more details.
- all All subpopulations with known sizes are used to scale the parameters, using a modified scaling procedure that standardizes the sizes so each population is weighted equally. Additional details are provided in Laga et al. (2021).
- weighted All subpopulations with known sizes are weighted according their correlation with the unknown subpopulation size. Additional details are provided in Laga et al. (2021)
- weighted\_sq Same as 'weighted', except the weights are squared, providing more relative weight to subpopulations with higher correlation.

#### Value

The named list containing the scaled log degree, degree, log prevalence, and size estimates

#### References

Zheng, T., Salganik, M. J., and Gelman, A. (2006). How many people do you know in prison, *Journal of the American Statistical Association*, **101:474**, 409–423

Laga, I., Bao, L., and Niu, X (2021). A Correlated Network Scaleup Model: Finding the Connection Between Subpopulations

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